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**PHYSICS**

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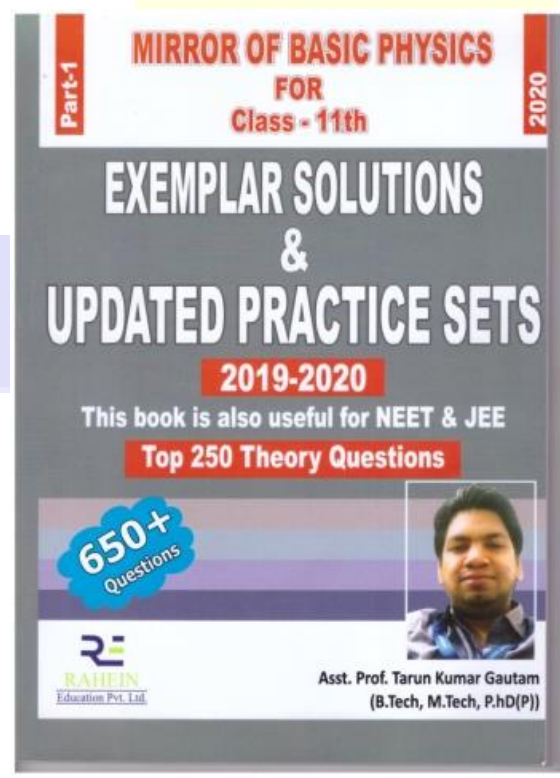
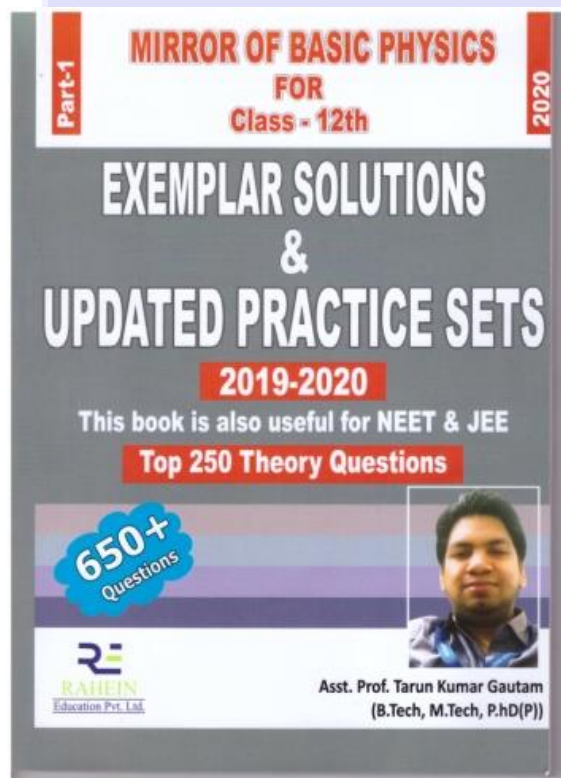
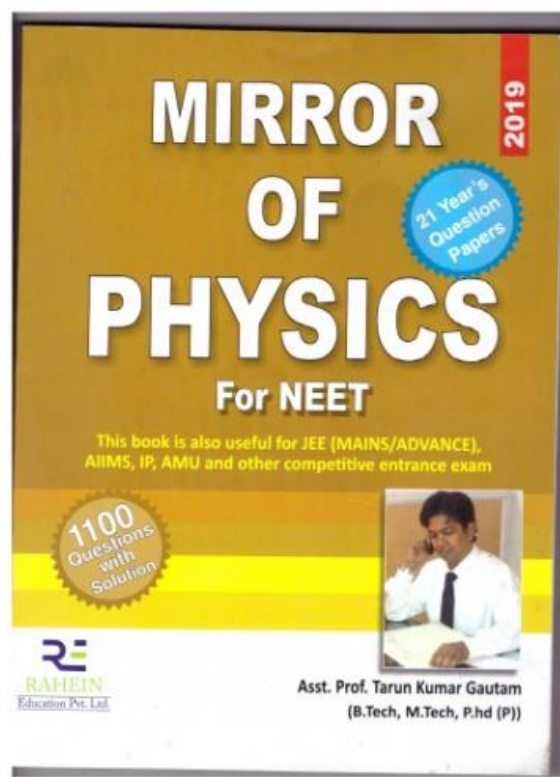
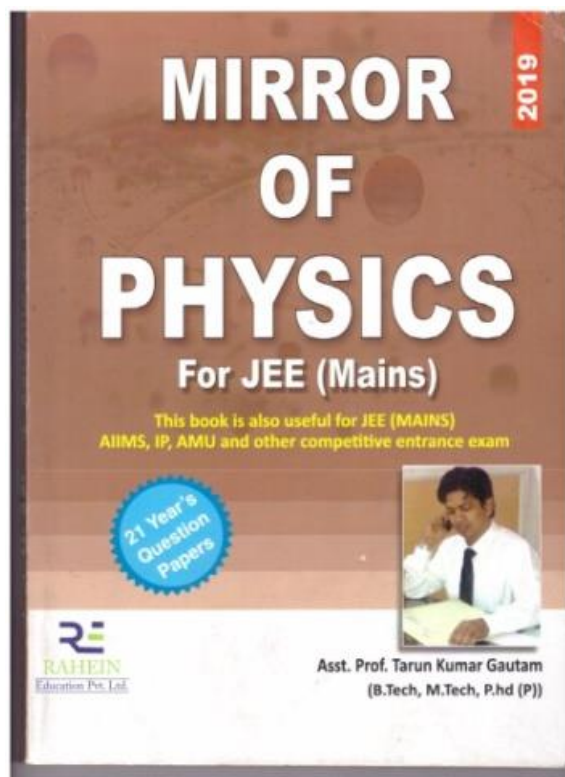
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## Chapter - 15

### [Waves]

#### \* Wave Motion

It is mean of transferring energy and momentum from one point to another without any actual transportation of matter between these points.

Thus, in wave motion, disturbance travels through some medium but the medium doesn't travel along with the disturbance.

#### Two types of mechanical waves

- 1) Transverse wave Motion
- 2) Longitudinal wave Motion

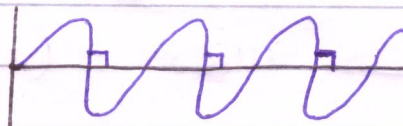
#### \* Transverse Wave Motion

It is the that motion in which individual particles of medium execute Simple Harmonic Motion about their mean position in a direction of perpendicular to the direction of propagation of wave motion.

Ex- Movement of Membrane of Tabla.

Ex- Movement of rope.

Transverse  
Wave Motion



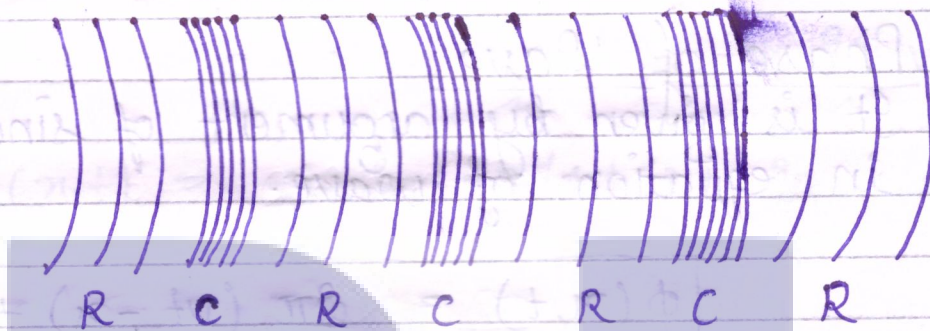
#### \* Longitudinal Wave Motion

It is the wave Motion in which individual



particles of medium execute Simple Harmonic motion about its mean position along the same direction along which wave is propagated as :

C  $\rightarrow$  Compression , R  $\rightarrow$  Rarefaction



### Wave Function

Function which describe mathematically the motion of wave pulse are called 'Wave Function'.

$$y = f(t)$$

### Periodic Wave Function

It is wave which repeats itself after a fixed interval of time is called 'Periodic Wave Function'

$$y(x, t) = y[x, (t + mT)]$$

$$\sin \theta = \sin(\theta + \pi)$$

### Harmonic Wave Function

The Harmonic waves corresponds to Periodic motion. It is called "Harmonic Wave function"



$$\rightarrow y(x,t) = r \sin \left[ \frac{2\pi}{\lambda} (vt-x) + \phi_0 \right]$$

$$\rightarrow y(x,t) = r \cos \left[ \frac{2\pi}{\lambda} (vt-x) + \phi_0 \right]$$

### \* Phase of Wave

It is given by argument of sine or cosine in equation of wave.

$$\phi(x,t) = \frac{2\pi}{\lambda} (vt-x) + \phi_0$$

$$\begin{cases} y = a \sin \phi \\ y = a \cos \phi \end{cases}$$

### \* Relation Between Particle Velocity & Wave Velocity

#### Equation of Wave

$$\rightarrow y(x,t) = r \sin \left[ \frac{2\pi}{\lambda} (vt-x) + \phi_0 \right]$$

if initial phase  $\phi_0 = 0$   
then,

$$y(x,t) = r \sin \left[ \frac{2\pi}{\lambda} (vt-x) \right]$$

velocity of particle :  $u(x,t)$

$$u(x,t) = \frac{dy(x,t)}{dt}$$



$$u(x,t) = y \cos \left[ \frac{2\pi}{\lambda} (vt - x) \right] \times \frac{2\pi}{\lambda} \times v$$

Particle acceleration:

$$a(x,t) = \frac{d[u(x,t)]}{dt}$$

$$a(x,t) = \frac{d}{dt} \left[ y \cos \left[ \frac{2\pi}{\lambda} (vt - x) \right] \times \frac{2\pi \cdot v}{\lambda} \right]$$

$$a(x,t) = -y \sin \left[ \frac{2\pi}{\lambda} (vt - x) \right] \frac{2\pi \cdot v}{\lambda} \times \frac{2\pi \cdot v}{\lambda}$$

$$a(x,t) = -y \sin \left[ \frac{2\pi}{\lambda} (vt - x) \right] \times \frac{4\pi^2}{\lambda^2} \times v^2$$

$$a(x,t) = -y \frac{4\pi^2}{\lambda^2} \times v^2$$

$$a(x,t) = -y \times 4\pi^2 \left( \frac{v}{\lambda} \right)^2$$

$$a(x,t) = -y \times 4\pi^2 \times v^2$$

$$a(x,t) = -y \times \omega^2$$

Note:  $\omega^2 = 2\pi v = (2\pi v)^2$

$$\omega^2 = 4\pi^2 \times v^2 \Rightarrow v = \lambda \cdot v$$

$$\frac{v}{\lambda} = v$$

then,

$$a(x,t) = -y \times 4\pi^2 \times v^2$$

$$a(x,t) = -y \omega^2$$

Note:

$$① \quad y(x,t) = y \sin \left[ \frac{2\pi}{\lambda} (vt - x) + \phi_0 \right]$$

$$② \quad \text{velocity of particle} \Rightarrow u(x,t) = -\frac{dy}{dt}$$

$$u(x,t) = y \cos \left[ \frac{2\pi}{\lambda} (vt - x) \right] \times \frac{2\pi}{\lambda} \cdot v$$

$$③ \quad \text{Acceleration of particle}$$

$$a(x,t) = \frac{du}{dt}$$

$$a(x,t) = -y \sin \left[ \frac{2\pi}{\lambda} (vt - x) \right] \times \frac{4\pi^2}{\lambda^2} \times v^2$$

$$a(x,t) = -y \omega^2$$

$$④ \quad \omega = 2\pi \nu = \frac{2\pi}{T}$$

$$⑤ \quad v = \lambda \nu$$

### Organ Pipe



Standing wave in closed organ pipe

$$\lambda = \frac{4L}{(2n-1)}$$

1) 1st Normal mode of vibration

$$n=1, \quad \lambda_1 = \frac{4L}{(2 \times 1 - 1)} = \frac{4L}{1}$$

$$L = \frac{\lambda_1}{4}$$



$$\boxed{\lambda_1 = \frac{V}{\nu_1} = \frac{V}{4L}} \quad \text{fundamental Note or Isoharmonic}$$

(ii) II<sup>nd</sup> Normal Mode of Vibration  
 $n=2, \lambda_2 = \frac{4L}{(2 \times 2 - 1)} = \frac{4L}{3}$

$$\boxed{\lambda_2 = \frac{V}{\nu_2} = \frac{3V}{4L}}$$

(iii) III<sup>rd</sup> Normal mode of Vibration  
 $n=3$

$$\lambda_3 = \frac{4L}{3} = \frac{4L}{5}$$

$$\nu_3 = \frac{V}{\lambda_3} = \frac{3V}{4L} = 5 \times \left[ \frac{V}{4L} \right] = 5 \nu_1$$

$$\nu_3 = 5 \nu_1$$

$$\boxed{\nu_n = (2n-1) \nu_1}$$

Standing wave in open Organ pipe

$$\boxed{\lambda = \frac{2L}{n}}$$

(i) I<sup>st</sup> Normal Mode of Vibration  
 $n=1, \lambda_1 = \frac{2L}{1} \quad \boxed{L = \frac{\lambda_1}{2}}$

$$\boxed{\lambda_1 = \frac{V}{\nu_1} = \frac{V}{2L}}$$

fundamental note or Isoharmonic



(ii) II<sup>nd</sup> normal mode of vibration  
 $n=2, \lambda_2 = \frac{2L}{2} = L$

$$v_2 = \frac{v}{\lambda_2} = \frac{v \times 2}{L \times 2} = 2 \left[ \frac{v}{2L} \right] = 2v_1$$

$$\boxed{v_2 = 2v_1}$$

Second Harmonic or first overtone

(iii) III<sup>rd</sup> normal mode of vibration  
 $n=3, \lambda_3 = \frac{2L}{3}$

$$v_3 = \frac{v}{\lambda_3} = \frac{3v}{2L} = 3 \times \left[ \frac{v}{2L} \right] = 3v_1$$

$$\boxed{v_3 = 3v_1}$$

$$\boxed{v_n = nv_1}$$

Standing wave in string

$$y_1 = \alpha \sin(\omega t - Kx)$$

$$y_2 = \alpha \sin(\omega t + Kx - \pi) = -\alpha \sin(\omega t + Kx)$$

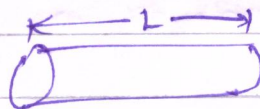
$$y = y_1 + y_2$$

$$y = \alpha [\sin(\omega t - Kx) - \sin(\omega t + Kx)]$$

$$\boxed{y = -2\alpha \cos x \sin \omega t}$$

$$\text{as, } \sin C - \sin D = 2 \cos \left[ \frac{C+D}{2} \right] \sin \left[ \frac{C-D}{2} \right]$$

at end point:-



$$x = L, y = 0$$

$$\sin kL = 0$$

$$\sin kL = \sin n\pi$$

$$kL = n\pi$$

$$\frac{2\pi}{\lambda} \cdot L = n\pi$$

$$\boxed{\lambda = \frac{2L}{n}}$$

Ist Mode of vibration

$$n=1, \lambda_1 = \frac{2L}{1} = 2L$$

$$\boxed{v_1 = \frac{v}{\lambda_1} = \frac{v}{2L}} \rightarrow v = \sqrt{\frac{I}{m}} \begin{matrix} \text{Tension} \\ \text{mass} \end{matrix}$$

$$\boxed{v_1 = \frac{1}{2L} \sqrt{\frac{I}{m}}}$$

called "fundamental note or Isoharmonic"

IInd Mode of vibration

$$n=2, \lambda_2 = \frac{2L}{2} = L$$

$$v_2 = \frac{v}{\lambda_2} = \frac{2}{2L} \sqrt{\frac{I}{m}} = 2 \times v_1$$

$$\boxed{v_2 = 2v_1}$$

Second Harmonic or Ist Overtone

$$\boxed{v_n = n v_1}$$

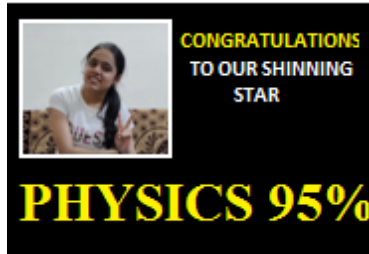




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